## MAE 208: Rube Goldberg Machine

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## Description



Starting by releasing a car from rest, the car will impact another object which will continue to affect other objects until the end of the machine. The function of our machine is to turn on a floor lamp using common household objects arranged into a Rube Goldberg Machine.

## Sketches



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O^{2}
$$

$$
1 \text { sttp } 3
$$



## Sketches



Step 7: books lined like dominoes fall and knock the ball


Step 8:ball rolls off table and hits the light switch

(3)

## Flow Chart

```
Input: Human
Release
Principle: Relative
Motion
Output: Can Rolling
```

Input: Car hitting
Input: Can hitting

Input: Basketball<br>falling<br>Principle: Projectile motion<br>Output: Lights on

Principle: General Planar Motion Output: Golf Ball Rolling

Input: Pendulum hits books
Principle: Central Impact
Output: Basketball falling
golf ball
Principle: Impulse Output: golf ball hits volleyball/basketball

## Input: String

 releases wrench Principle: rotational motionOutput: wrench hits book

## Input: Golf ball hits volleyball/basketball Principle: Conservation of momentum <br> Output: Ball rolls down <br> stairs

##  <br> I

Input: Basketball hits water bottle Principle: oblique impact Output: water bottle falls down freeing string

## Step ½

## Components Used:

Step 1: Table, Two small pullback cars

Bobby. "How Does A Pull Back Toy Motor Work." News about Energy Storage, Batteries, Climate Change and the Environment, UpsBatteryCenter, 8 Aug. 2014,
www.upsbatterycenter.com/blog/pull-back-toy-moto r-work/.
"Rotational-Linear Parallels." Moment of Inertia, hydrogen.physik.uni-wuppertal.de/hyperphysics/hy perphysics/hbase/mi.html.

Step 2: Table, An object that can roll along a straight line (Aluminum Can)

Assumptions Made:
Table Height $=0.7 \mathrm{~m}$
Car 1 Mass $=287 \mathrm{~g}$
Car 2 Mass $=302 \mathrm{~g}$
Aluminum Can Mass $=384 \mathrm{~g}$
Car 1 is pulled back farther than Car 2

## Step 1: Moving Cars (Relative Motion)

Focus: Two cars are released into motion. They move relative to each other at different speeds while one sets an aluminum can into motion at the end of the step.

Input: Human input to release both cars.

Output: Car 1 crashes into the aluminum can to set it in motion.

Solved Variables:
$s_{1}=0.2 \mathrm{~m}, \mathrm{t}=1 \mathrm{~s} \Rightarrow \mathrm{v}_{1}=\mathrm{s}_{1} / \mathrm{t}=0.2 \mathrm{~m} / \mathrm{s}$
$s_{2}=0.13 \mathrm{~m}, \mathrm{t}=1 \mathrm{~s} \Rightarrow \mathrm{v}_{2}=\mathrm{s}_{2} / \mathrm{t}=0.13 \mathrm{~m} / \mathrm{s}$
$v_{1 / 2}=v_{1}-v_{2}=0.07 \mathrm{~m} / \mathrm{s}$

## Step 2: Rolling Can (General Planar Motion)

Focus: Can rolls across table to tap a golf ball at the end to set it in motion.

Input: Car hits the can to set it in motion.
Output: Can hits golf ball to set it in motion.
Solved Variables: $\mathrm{I}=\mathrm{MR}^{2} / 2$
$M=0.384 \mathrm{~kg}, \mathrm{R}=0.05 \mathrm{~m} \Rightarrow \mathrm{I}=4.8 \times 10^{4} \mathrm{kgm}^{2}$
$\mathrm{m}_{\text {car }} \mathrm{v}_{\text {car1 }}+\mathrm{m}_{\text {can }} \mathrm{v}_{\text {can1 }}=\mathrm{m}_{\text {car }} \mathrm{v}_{\text {car2 }}+\mathrm{m}_{\text {can }} \mathrm{v}_{\text {can2 }}$
$0.287 * 0.2=0.287 * 0.09+0.384 \mathrm{v}_{\text {can2 }} \Rightarrow \mathrm{v}_{\text {can2 }}=0.08 \mathrm{~m} / \mathrm{s}$
$\omega=\mathrm{v} / \mathrm{r} \Rightarrow \omega=1.64 \mathrm{rad} / \mathrm{s}$

## Step 3/4

FloVolleyball Staff. "Volleyball Facts and Dimensions." FloSports. N.p., 11 Jan. 2017. Web. 18 Apr. 2020.

Craig, Dexter \& May, Stephen. Teed Off! How a Golf Ball Really Works. The Virtual Golfer. 1995

Gutmann, Mindy . "The Physics Of Sports." N.p., 9 June 1997. Web. 21 Apr. 2020.

## Components Used:

3 - table of reasonable height, a small dense ball (golf ball), an angled surface (calf raiser), and a flat pillow on top of the calf raiser

4 - books to guide the small ball (golf ball), and a larger ball(outdoor volleyball) light enough to be knocked over by the small ball

## Assumptions Made:

Table Height $=69.215 \mathrm{~cm}$
Golf Ball Mass $=45.93 \mathrm{~g}$
Volleyball Mass $=270 \mathrm{~g}$
Angle of Surface $=30^{\circ}$
Angle of Impact of balls $=90^{\circ}$
Time of impact between golf ball and pillow $=0.05 \mathrm{sec}$ $\mathrm{e}=0.873$

## Step 3: Golf ball rolls of table and hits the angled surface (impulse)

Focus: Golf ball falls off the table and hits the pillow on top of the angled surface, redirecting the golf ball.

Input: Can hits the golf ball and knocks it off the table
Output: Golf ball bounces off the angled pillow towards the volleyball/stairs

Solved Variables:

$$
m v_{i}+\int F d t=m v_{f}
$$

$\left|v_{f}\right|=1.469 \mathrm{~m} / \mathrm{s}$
$\mathrm{F}_{\text {pillow }}=4.397 \mathrm{~N}$

## Step 4: Golf ball hits volleyball (Conservation of Momentum)

Focus: Golf ball hits the volleyball, knocking it off the ledge of the stairs to roll down.

Input: Golf ball bouncing off the angled surface hits the volleyball.

Output: Volleyball rolls off the ledge and down the stairs

Solved Variables:

$$
\begin{gathered}
m_{g} v_{i . g .}+m_{v} v_{i . v .}=m_{g} v_{f . g .}+m_{v} v_{f . v .} \\
E=\left(v_{f g}-v_{f v}\right) /\left(v_{i v}-v_{i g}\right)
\end{gathered}
$$

$v_{i, g}=0.7354 \mathrm{~m} / \mathrm{s}$
$\mathrm{v}_{\mathrm{i}, \mathrm{y}}=0 \mathrm{~m} / \mathrm{s}$
$\mathrm{v}_{\mathrm{f}, \mathrm{g}}=-0.924 \mathrm{~m} / \mathrm{s}$
$v_{f, v}=0.282 \mathrm{~m} / \mathrm{s}$

## Step 5 and 6

Persson, Jonas. "Measure the Coefficient of Restitution for Sports Balls." Physics Education, www.academia.edu/7888446/Measure the coefficient of restitution for sports balls.
"Geode Rose: S'well® Bottle Official: Reusable Insulated Water Bottles." S'we//® Official,
www.swell.com/products/swell/bottles/geode-rose/?\&gclid =EAlaIQobChMI7eP0xLTw6AIViorICh3oeAAYEAQYAiAB EgL8-_D_BwE\&gclsrc=aw.ds.

Components that could be used:
5 - an item that could froll/slide down stairs (box, ball, basket, bucket) and an item heavy enough to hold a string taught and tall enough to fall over when hit (water bottle, book, cups, jug)

6 - tall item that string can be tied to (ladder, shelf, chair, stool, ceiling), a string (yarn, rope, fishing line), an object that can be tied to the string (tape, wrench, hammer, small water bottle), and an item that can be knocked down (book, water bottle, box)

Assumptions made:
5 - coefficient of restitution $=.87$; mass of basketball $=$ .625 kg ; mass of water bottle $=.787$; basketball hits water bottle at a 45 degree angle, height of stairs = .635 m , assume no friction when ball rolls down stairs

6 - radius $=.508 \mathrm{~m}$, initial height $=.9114 \mathrm{~m}$, final height $=.7112 \mathrm{~m}$

## Step 5: Basketball hits water bottle (oblique impact)

Focus: water bottle falls over to the side so that the it is on top of is freed

Input: the basketball has velocity after rolling down the steps

Output: the string is no longer holding the wrench at an angle on the pendulum
$\mathrm{mgh}=1 / 2 \mathrm{mv}^{2} \quad \mathrm{v}=\sqrt{ } 2 \mathrm{gh} \quad \mathrm{v}=\sqrt{ } 2(9.81)(.635)=3.53 \mathrm{~m} / \mathrm{s}$
$\mathrm{V}_{\mathrm{ax}}=3.53 \cos (45)=2.5 \quad \mathrm{~V}_{\mathrm{ay}}=3.53 \sin (45)=2.5$
$\mathrm{e}=\left(\mathrm{V}_{\mathrm{bx} 2}-\mathrm{V}_{\mathrm{ax} 2}\right) /\left(\left(\mathrm{V}_{\mathrm{ax} 1}-\mathrm{V}_{\mathrm{bx} 1}\right) \quad .87(2.5-0)=\mathrm{V}_{\mathrm{bx} 2}-\mathrm{V}_{\mathrm{ax} 2}\right.$
$M_{a} V_{a x 1}+M_{b} V_{b x 1}=M_{a} V_{a x 2}+M_{b} V_{b x 2}$ $.625(2.5)+.787(0)=.625 \mathrm{~V}_{\mathrm{a} \times 2}+.787 \mathrm{~V}_{\mathrm{bx} 2}$ $\mathrm{v}_{\mathrm{ax} 2}=.472 \mathrm{~m} / \mathrm{s}$

$$
v_{\mathrm{b} \times 2}=2.647 \mathrm{~m} / \mathrm{s}
$$

$\mathrm{M}_{\mathrm{a}} \mathrm{V}_{\mathrm{ay} 1}=\mathrm{M}_{\mathrm{a}} \mathrm{V}_{\mathrm{ay} 2}$

$$
M_{b} V_{b y 1}=M_{b} V_{b y 2}
$$

$V_{b y 2}=0 \mathrm{~m} / \mathrm{s}$

## Step 6: Pendulum swings and hits book (rotational motion)



Focus: the potential energy created by the change in height of the wrench translates into kinetic energy giving the wrench speed

Input: the string tied to the wrench is no longer taut once the water bottle falls, and the wrench falls creating kinetic energy

Output: the wrench hits the textbook at the bottom of the pendulum
$m g \Delta h=.5 l \omega^{2}=.5 \mathrm{mr}^{2}(\mathrm{v} / \mathrm{r})^{2}=.5 m v^{2}$
$V=\sqrt{ } 2 g h \quad v=\sqrt{ } 2(9.81)(.9114-.7112)$
$V=1.982 \mathrm{~m} / \mathrm{s}$
$\omega=\mathrm{v} / \mathrm{r}=1.982 / .508$
$\omega=3.902 \mathrm{rad} / \mathrm{s}$

## Step 7/ 8

Alexander, Jason, et al. Characterising the Physicality of Everyday Buttons.

Nilsen, Lottie, and Denver Post. "E-Textbooks Win Fans, but Some Students Still Prefer Paper." The Denver Post, The Denver Post, 4 May 2016,
www.denverpost.com/2012/04/14/e-textbooks-win-fans-b ut-some-students-still-prefer-paper-3/.

Winkler, Eric. "What Is the Mass of Basketball?" Dunk or Three, 20 Mar. 2020,
dunkorthree.com/mass-of-basketball/.

## Components Used:

7 - somewhat large books (textbooks), table of reasonable height, a decently-sized object that can roll (basketball, soccer ball)

8 - table of reasonable height, object that falls off the table (basketball, soccer ball), a lamp/light with a foot switch

## Assumptions Made:

7 - Mass of the books: $\sim 1.6 \mathrm{~kg}$, Mass of the basketball: 625 g , Coefficient of restitution $=0.87$

8 - Mass of the basketball: 625 g , Table height: 70 cm , minimum force required to push the light switch: 287.9 g +- 376.3 g

## Step 7: Books create a chain reaction and hits basketball (central impact)

Focus: Books fall in a chain reaction like dominoes

Input: Pendulum hits the books, causing them to fall over

Output: Books will hit the basketball, pushing it off the table

$$
\begin{aligned}
& \text { Equations: (assuming } \left.v_{\text {book, } 1}=2 \mathrm{~m} / \mathrm{s}\right) \\
& e=\left(v_{\text {ball,2 }}-v_{\text {book, }, 2}\right) /\left(v_{\text {book, } 1}-v_{\text {ball, } 1}\right) \\
& 0.87=\left(v_{\text {ball,2 }}-v_{\text {book, } 2}\right) /(2-0) ; 1.74=v_{\text {ball, } 2}-v_{\text {book,2 }} \\
& m_{\text {book }} v_{\text {book }, 1}+m_{\text {ball }} v_{\text {ball, } 1}=m_{\text {book }} v_{\text {book }, 2}+m_{\text {ball }} v_{\text {ball,2 }} \\
& (1.6)(2)+0=(1.6)\left(v_{\text {book,2 }}\right)+(0.625)\left(v_{\text {ball,2 }}\right) \\
& v_{\text {ball,2 }}=2.69 \mathrm{~m} / \mathrm{s}, v_{\text {book }, 2}=0.95 \mathrm{~m} / \mathrm{s}
\end{aligned}
$$

## Step 8: Basketball falls off the table, hitting the light switch and turning on the lamp (projectile motion)



Focus: Basketball will fall and hit the light switch on the ground

Input: Books hit the basketball, causing it fall off the table

Output: The lamp switch is hit, turning on the lamp
Equations:
$y=v_{0, y}{ }^{* t}+0.5 a t^{\wedge} 2$
$0.7 m=0 * t+(0.5)(-9.81) t^{\wedge} 2, t=0.377 s$
$F_{\text {ball, }}=m a=(0.625 \mathrm{~kg})(9.81)=6.131 \mathrm{~N}$

Video Step 1

Video Step 3

Video of Step 6

Video of Step 8

